

# A New Simple and Effective Procedure for SiPM Electrical Parameter Extraction

Davide Marano, Giovanni Bonanno, Salvatore Garozzo, Alessandro Grillo, and Giuseppe Romeo

**Abstract**—Silicon photomultipliers (SiPMs) are emerging semiconductor-based photosensors, addressing the challenge of low-light detection down to the single-photon counting level. A design of high-performance front-end electronics for SiPM readout requires the development of accurate electrical models. Numerous SiPM reliable models have matured in recent years; however, circuit parameter extraction is rather cumbersome and involves extensive measurement steps to be performed. Starting from a recently developed model of the SiPM device coupled to the conditioning electronics, a new effective analytical procedure is, here, devised for extracting the SiPM model parameters from experimental measurements. The proposed extraction technique is applied to a  $3 \times 3\text{-mm}^2$  SiPM sensor, and is validated by comparing SPICE simulations and measurement results. Independent cross-check validation based on experimental tests corroborates the effectiveness of the adopted extraction procedure.

**Index Terms**—Analytical model, circuit parameters, front-end electronics, pulse waveform, transient response.

## I. INTRODUCTION

**I**N LIGHT of the contemporary evolution of astrophysics, nuclear science and medical imaging, the development of new silicon photomultiplier (SiPM) detectors is being devoted an ever-increasing amount of attention in recent years. The number of scientific and technical applications which benefit from the peculiar advantages of solid-state sensors is continuously growing over time, fostered by the rapid industrial advancement of modern semiconductor technologies.

SiPMs basically consist of a parallel array of single-photon avalanche photodiodes operating above breakdown (in the so-called Geiger-mode) in series with an integrated quenching or ballast resistance. In principle, for a SiPM proper operation, a biasing circuit and a read-out amplifier are required, as schematically shown in the simplified diagram in Fig. 1.

In the steady-state condition, no current flows through the device terminals, and the external supply  $V_{BIAS}$  sets the SiPM operating point at a voltage which is typically 10-20% greater than its breakdown potential. When an optical photon strikes the active surface of the  $n$ -th photodiode, the device microcell

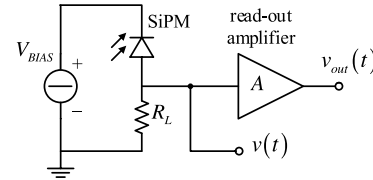


Fig. 1. Schematic overview of a typical SiPM read-out circuit.

undergoes a Geiger discharge and produces a short pulse current,  $i_n(t)$ , resulting in a voltage pulse signal at the SiPM output node,  $v_n(t) = GR_L i_n(t)$ , where  $G$  is the avalanche multiplication factor and  $R_L$  is the sensing resistance. If a given number of photons triggers  $N_f$  avalanches in  $N_f$  different pixels, then the overall sensor response would be the analog superposition of  $N_f$  individual pulse shapes. Under the assumption of uniform gain among the individual microcells,  $N_f$  triggered pixels would deliver an output voltage signal expressed as

$$v(t) = \sum_{n=1}^{N_f} v_n(t) = \sum_{n=1}^{N_f} GR_L i_n(t) = N_f [GR_L i(t)], \quad (1)$$

hence theoretically permitting the detection and measurement of optical signals at the single photon counting level.

In order to exploit the excellent intrinsic SiPM timing resolution, the development of specialized, highly integrated read-out electronics is required. However, the number of front-end architectures specifically designed for SiPM read-out is fairly poor, and considerable effort is thus being involved in finding newer and more performing solutions in terms of dynamic speed and time resolution. To this purpose, a substantial benefit for circuit designers is represented by the possibility of performing accurate circuit-level simulations of the SiPM detector coupled to the conditioning electronics, allowing to choose the optimal characteristics of the front-end systems for optimizing overall time performance.

In this scenario, the rising number of emerging applications demanding best theoretical dynamic speed and single-photon time resolution, as well as the contextual request for suitable integrated front-end electronics, have recently provided motivation and stimuli for in-depth research studies on the SiPM output dynamic response [1]–[12], allowing a detailed analytical description of the device behavior.

A traditionally accepted electrical model of a SiPM detector is shown in Fig. 2. The model is able to simulate the discharge of  $N_f$  active pixels over a number  $N$  of total microcells.

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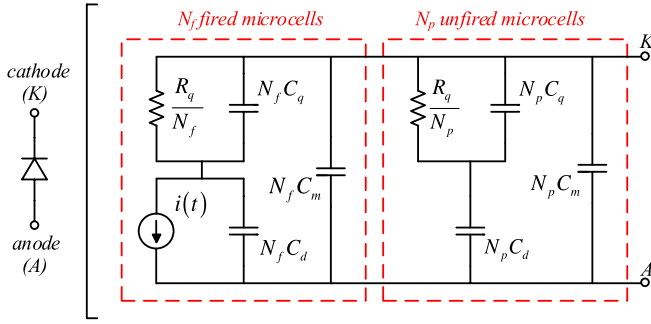


Fig. 2. Traditional electrical model of a SiPM detector.

The circuit is divided into an active part for the  $N_f$  fired pixels and a passive block for the remaining  $N_p = N - N_f$  unfired microcells. For an individual pixel,  $C_d$  is the junction capacitance of the diode depletion layer,  $R_q$  and  $C_q$  are respectively the ballast resistance and stray capacitance, while  $C_m$  accounts for all interconnect capacitances across the SiPM terminals.

The Geiger discharge of the single firing microcell, caused by either an impinging photon or thermal carriers generation, is mimicked by the time-dependent source  $i(t)$ , simulating the photodiode exponential decay current and expressed as

$$i(t) = \frac{Q}{\tau_d} e^{-\frac{t}{\tau_d}}, \quad (2)$$

where  $\tau_d$  is the quenching time constant of the avalanche discharge and  $Q$  is the overall amount of charge delivered by the fired pixel, which is represented by the integral of the photodiode current over time and calculated as the product between the excess bias voltage  $V_{OV}$  and the pixel capacitance  $C_{pixel}$

$$Q = \int_0^{+\infty} i(t) dt = C_{pixel} V_{OV} = (C_d + C_q) (V_{BIAS} - V_{BD}), \quad (3)$$

being  $V_{BD}$  the device breakdown potential.

The number of unit electron charges originated in response to a photon absorption (or a thermally ignited avalanche), denotes the multiplication factor  $G$  of the Geiger discharge and is usually referred to as the SiPM gain, whose typical expression as a function of the operating voltage is then

$$G = \frac{Q}{q} = \frac{C_d + C_q}{q} (V_{BIAS} - V_{BD}). \quad (4)$$

where  $q$  denotes the elementary electron charge.

The effectiveness of the SiPM model, along with its ability to perform reliable software simulations, is strongly related to the choice of the circuit parameters, whose derivation strategy hence assumes a significant role in establishing predictive capability of the adopted model. Despite the inherent simplicity and accuracy of the SiPM model in Fig. 2, the related parameter extraction methodology is somewhat complex and burdensome, and needs extensive and time-consuming measurement steps to be performed [13]–[17]. More specifically:

- a) the breakdown voltage  $V_{BD}$  is estimated by the measured detector current as a function of the reverse bias

voltage, or else from the extrapolation of the  $x$ -axis intercept of a linear fit in a gain plot against the operating voltage;

- b) parameter  $\tau_d$  is evaluated from the measured rise time of the amplified SiPM signal;
- c) resistor  $R_q$  is obtained through the slope of the static I-V characteristics of the device in its forward region;
- d) the terminal capacitance  $C_{pixel}$  is extracted by evaluating the overall charge injected by the fired pixels in a signal charge histogram, or alternatively through the slope of a linear fit in a gain plot versus the operating voltage;
- e) the individual capacitive components  $C_d$  and  $C_q$ , and the grid parasitic capacitance  $C_p$ , are assessed by fitting the complex impedance of the SiPM model to the measured impedance of the reverse-biased device.

In addition, parameter extraction does not take into account the effect of the read-out electronics on the shape of the SiPM response, which might have a non-negligible influence on the value of the estimated model parameters.

In the following, a new effective and straightforward methodology for extracting the SiPM model parameters is devised, relying on two simpler measurement steps:

- a) determination of  $R_q$  by means of a linear fit to the measured forward I-V characteristics;
- b) extraction of all remaining electrical parameters through the measurement and analytical data fitting of the amplified SiPM transient response.

The proposed procedure is based on a recently adopted full model of the SiPM detector with its coupled read-out amplifier [1], and is then validated and cross-checked by comparison with experimental results.

The remainder of the paper is organized as follows. In Section II, the enhanced SiPM model resulting from coupling the device to its read-out amplifier is briefly reviewed. The novel procedure for SiPM parameter extraction is addressed in Section III. In Section IV, experimental validation of the adopted strategy is performed. Section V provides cross-check results corroborating the effectiveness of the proposed methodology. Finally, the authors' conclusions are drawn in Section VI.

## II. REVIEW OF THE FULL SiPM ANALYTICAL MODEL

Fig. 3 depicts the linear small-signal circuit of the electrical model of the SiPM detector when coupled to its read-out electronics. The SiPM equivalent circuit is directly derived from the model in Fig. 2 endorsing capacitances  $N_f C_m$  and  $N_p C_m$  into the single capacitive contribution  $C_p = N C_m$ . The equivalent circuit of the front-end electronics is based on the typical single-pole model of a generic read-out amplifier, where  $R_{in}$  and  $C_{in}$  are respectively the equivalent input resistance and capacitance,  $g_m R_{out}$  is the DC gain  $A$ , while the product  $R_{out} C_{out}$  represents the reciprocal of the 3dB cut-off angular frequency resulting from dominant-pole approximation.

The trans-resistive small-signal transfer function of the circuit model in Fig. 3 in the complex  $s$ -frequency

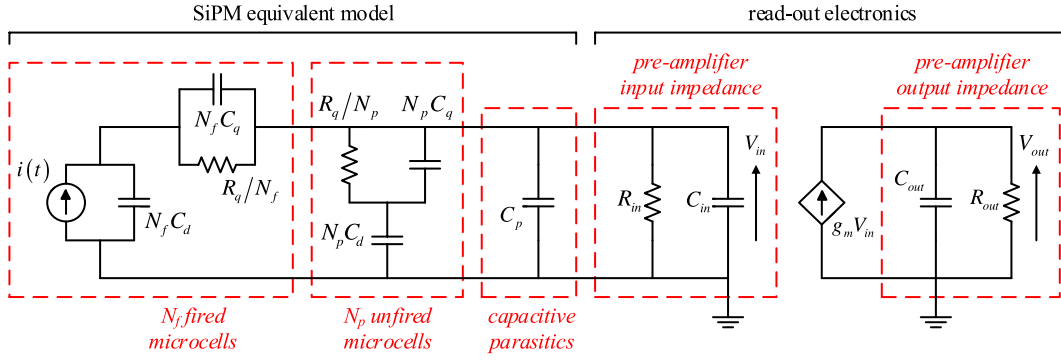


Fig. 3. Linear small-signal equivalent model of the SiPM detector coupled to the front-end electronics.

domain is

$$F(s) = \frac{V_{out}(s)}{I(s)} = F_0 \frac{1 + s\tau_z}{(1 + s\tau_{p1})(1 + s\tau_{p2})(1 + s\tau_{out})}, \quad (5)$$

with  $F_0 = g_m R_{in} R_{out}$ , and the circuit time constants given by

$$\tau_z = R_q C_q, \quad (6)$$

$$\tau_{p1} = R_q (C_d + C_q) + R_{in} (C_{in} + N C_d), \quad (7)$$

$$\tau_{p2} = \frac{R_{in} R_q [N C_d C_q + (C_{in} + C_p) (C_d + C_q)]}{R_q (C_d + C_q) + R_{in} (C_{in} + N C_d)}, \quad (8)$$

$$\tau_{out} = R_{out} C_{out}. \quad (9)$$

Solving (5) for  $V_{out}(s)$ , substituting the  $s$ -domain expression of  $i(t)$  in (2), and then inverse Laplace transforming, the final SiPM single-photoelectron time response is derived as

$$v_{out}(t) = k \left( A_d e^{-\frac{t}{\tau_d}} + A_{p1} e^{-\frac{t}{\tau_{p1}}} + A_{p2} e^{-\frac{t}{\tau_{p2}}} + A_{out} e^{-\frac{t}{\tau_{out}}} \right), \quad (10)$$

in which the static multiplicative term is

$$k = F_0 Q = q F_0 G, \quad (11)$$

and the four exponential coefficients are expressed by

$$A_d = \frac{\tau_d (\tau_d - \tau_z)}{(\tau_d - \tau_{p1}) (\tau_d - \tau_{p2}) (\tau_d - \tau_{out})}, \quad (12)$$

$$A_{p1} = \frac{\tau_{p1} (\tau_{p1} - \tau_z)}{(\tau_{p1} - \tau_d) (\tau_{p1} - \tau_{p2}) (\tau_{p1} - \tau_{out})}, \quad (13)$$

$$A_{p2} = \frac{\tau_{p2} (\tau_{p2} - \tau_z)}{(\tau_{p2} - \tau_d) (\tau_{p2} - \tau_{p1}) (\tau_{p2} - \tau_{out})}, \quad (14)$$

$$A_{out} = \frac{\tau_{out} (\tau_{out} - \tau_z)}{(\tau_{out} - \tau_d) (\tau_{out} - \tau_{p1}) (\tau_{out} - \tau_{p2})}. \quad (15)$$

The SiPM output response is a quadruple-exponential function exhibiting a rising ( $\tau_d$ ), quenching ( $\tau_{p2}$ ), and recovery ( $\tau_{p1}$ ) phase, and also accounting for the shaping effects of the coupled front-end electronics ( $\tau_{out}$ ).

The overall charge  $Q$  released by the triggered microcells and delivered to the output signal is proportional to the integral of the SiPM response over time, and is merely related to the pixel capacitance and applied excess bias voltage,

as established in (3). This means that, for the same load resistance,  $R_{in}$ , and pre-amplifier gain factor,  $g_m R_{out}$ , the integral of  $v_{out}(t)$  with respect to time should be independent of the frequency characteristics of the front-end electronics ( $\tau_{out}$ ). In fact,

$$\int_0^{+\infty} v_{out}(t) dt = k (A_d \tau_d + A_{p1} \tau_{p1} + A_{p2} \tau_{p2} + A_{out} \tau_{out}) = k \quad (16)$$

since the sum of the terms in round brackets equals unity.

The achieved expression for  $v_{out}(t)$  in (10) also satisfies the initial- and final-value conditions, as

$$v_{out}(0) = k (A_d + A_{p1} + A_{p2} + A_{out}) = 0, \quad (17)$$

$$\lim_{t \rightarrow +\infty} v_{out}(t) = 0. \quad (18)$$

A remarkable advantage of the obtained analytical relationship of the SiPM output waveform is that it properly accounts for the effect of the coupled front-end electronics, modulating the shape of the basic SiPM pulse ( $v(t)$  in Fig. 1) and playing a major role in determining time performance, dynamic range and photon counting resolution of the detection system independently of the particular fabrication technology. Indeed, relying on the general pre-amplifier macro-model in Fig. 3, the SiPM front-end electronics can be functionally associated to the major relevant model parameters regardless of the specific inner circuit topology and architecture.

Based on the above model and analytical analysis, the new procedure for SiPM parameter extraction is now developed.

### III. MODEL PARAMETER EXTRACTION PROCEDURE

The first step of the proposed procedure consists in the determination of the quenching resistance  $R_q$ . Biasing the SiPM detector in its forward region, the resulting I-V characteristics should obey to the following law

$$V = \frac{R_q}{N} I + \eta V_T \ln \left( \frac{I}{N I_S} \right), \quad (19)$$

in which  $V_T$  and  $\eta$  are respectively the thermal voltage and the emission coefficient of the photodiode junction, and  $I_S$  is the photodiode reverse saturation current.

The SiPM forward I-V curves present two distinct parts: an initial phase when the current is governed by the typical diode exponential behavior as a function of the applied voltage, and a subsequent phase in which the quenching resistor becomes the dominant contribution and limits the forward current to an almost linear growth. The equivalent resistance  $R_q/N$  can thus be evaluated from the slope of the linear part, from which the quenching resistor value can be easily extracted.

As to the succeeding measurement step, referring to Fig. 1, the SiPM single-photoelectron response,  $v_{out}(t)$ , is recorded on a digital oscilloscope with the detector under test subjected to dark count events, ensuring the most probable event to be the firing of a single pixel. For a fixed external voltage  $V_{BIAS}$ , histograms of the maximum pulse heights are digitally captured according to the number of cells triggering for each event. Afterwards, events with equal number of fired cells are grouped and averaged to form a single pulse waveform.

Model parameters of the read-out section are obtained from the knowledge of the specific amplifier adopted. In particular, the input capacitance  $C_{in}$  is typically available from the manufacturer datasheet, whilst the input and output resistances,  $R_{in}$  and  $R_{out}$  respectively, along with the  $-3\text{dB}$  small-signal bandwidth  $f$  can be achieved from the simulation model once the desired amplifier configuration and closed-loop gain  $A$  are selected. Subsequently, transconductance  $g_m$  is derived from the equation  $A = g_m R_{out}$ , and capacitance  $C_{out}$  is evaluated by means of the well-known relationship

$$f = \frac{1}{2\pi R_{out} C_{out}}, \quad (20)$$

hence allowing the values of  $F_0$  and  $\tau_{out}$  to be determined.

At this point, a nonlinear regression technique is applied to the measured SiPM output response, and the collected data of  $v_{out}(t)$  are fitted with a fourth-exponential function  $g$  obtained substituting expressions (11)-(15) into (10), yielding

$$v_{out} = g(G, \tau_d, \tau_{p1}, \tau_{p2}, \tau_z), \quad (21)$$

in order to find the unknown parameters  $G$  and  $\tau_d, \tau_{p1}, \tau_{p2}, \tau_z$ .

Once the three time constants  $\tau_{p1}, \tau_{p2}$ , and  $\tau_z$  are evaluated, by means of the relevant analytical expressions in (6)-(8), the values of the three capacitors  $C_d, C_q$ , and  $C_p$  can be easily extracted according to the following relationships

$$C_d = \frac{\tau_{p1} - \tau_{in} - \tau_z}{R_q}, \quad (22)$$

$$C_q = \frac{\tau_z}{R_q}, \quad (23)$$

$$C_p = \frac{NR_{in}(\tau_{p2} - \tau_z) + R_q(\tau_{p2} - \tau_{in})}{R_{in}R_q}, \quad (24)$$

where  $\tau_{in}$  represents the product between  $R_{in}$  and  $C_{in}$ .

Finally, from the known value of  $G$  and using the estimated values of  $C_d$  and  $C_q$  in (22)-(23), the SiPM breakdown potential is easily obtained from (4) as

$$V_{BD} = V_{BIAS} - \frac{qG}{C_d + C_q}. \quad (25)$$

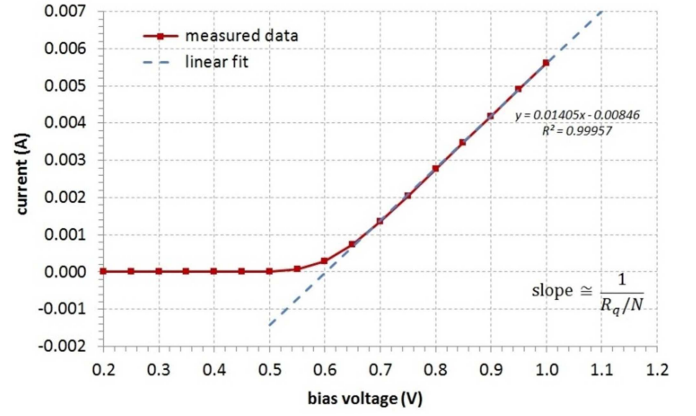


Fig. 4. Fitting of the linear part of the SiPM forward I-V characteristics, from which the value of the quenching resistor  $R_q$  is extracted.

#### IV. VALIDATION OF THE EXTRACTION PROCEDURE

The adopted extraction procedure is exploited to derive the electrical model parameters of a  $3 \times 3\text{-mm}^2$  multi-pixel photon counter detector supplied by Hamamatsu Photonics, featuring a  $50\text{-}\mu\text{m}$  cell size and 3600 elementary pixels. The breakdown voltage declared in the manufacturer datasheet ranges around  $65\text{V}$  at room temperature.

Data-fitting procedures are performed in the MATLAB environment using the command `lsqcurvefit()`, which enables measurement data arrays to be fitted with complex non-linear functions in least-squares sense.

The SiPM static I-V characteristics are illustrated in Fig. 4, along with a linear fitting regression applied to the measured data points corresponding to an operating voltage higher than  $0.7\text{V}$ . By the slope of the linear fit, a value of  $256.2\text{k}\Omega$  is extracted for the quenching resistor  $R_q$ .

To obtain the remaining parameters of the SiPM model, the experimental apparatus illustrated in Fig. 1 is assembled, with  $R_L = 50\Omega$  and  $V_{BIAS} = 68\text{V}$ . A THS3201 read-out pre-amplifier is used in non-inverting feedback configuration, with a  $1\text{-pF}$  input capacitance and a  $\sim 40\text{-dB}$  nominal gain factor, for which a closed-loop bandwidth of  $\sim 50\text{-MHz}$  is achieved from simulations. The measured SiPM pulse waveforms are acquired on a Lecroy digital oscilloscope characterized by a  $4\text{-GHz}$  bandwidth, a  $40\text{-GS/s}$  sampling rate, and an intrinsic  $0.5\text{-mV}$  baseline noise. SiPM single-photoelectron responses are captured with the detector lodged in a dedicated light-tight box to prevent accidental light exposure. Measurements are executed at room temperature.

The estimated parameters resulting from the fit between the experimental pulse waveform and the quadruple-exponential function in (21) are reported in Table I. Finally, according to the analytical expressions derived in Section III, the values of the SiPM model capacitances are calculated, together with the detector breakdown voltage. The extracted electrical parameters of the SiPM model in Fig. 2 are summarized in Table II.

To validate the above procedure, the circuit in Fig. 1 is implemented in SPICE using the SiPM model in Fig. 2 with the cascaded read-out pre-amplifier, as shown in Fig. 5.



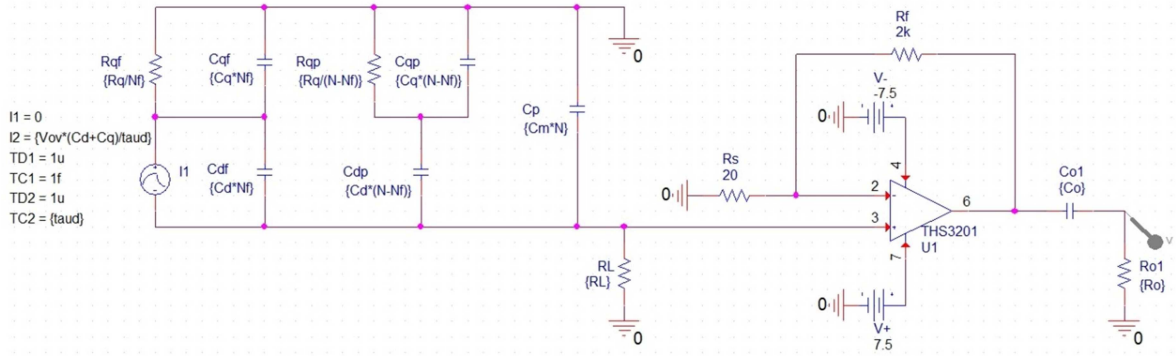


Fig. 5. Implemented SPICE-level model of the SiPM detector driven by a voltage non-inverting feedback amplifier.

TABLE I  
PARAMETERS OF THE SiPM FITTING FUNCTION IN (21)

Parameter	Value
$\tau_d$	$(0.25 \pm 0.03)$ ns
$\tau_{p1}$	$(40.09 \pm 0.05)$ ns
$\tau_{p2}$	$(1.65 \pm 0.01)$ ns
$\tau_z$	$(3.04 \pm 0.02)$ ns
$G$	$(1.68 \pm 0.03) \times 10^6$

TABLE II  
ELECTRICAL PARAMETERS OF THE SiPM MODEL IN FIG. 2

Parameter	Value
$R_q$	$(256.2 \pm 0.7)$ k $\Omega$
$C_d$	$(86.1 \pm 0.6)$ fF
$C_q$	$(12.8 \pm 0.2)$ fF
$C_p$	$(2.7 \pm 0.3)$ pF
$V_{BD}$	$(65.2 \pm 0.1)$ V

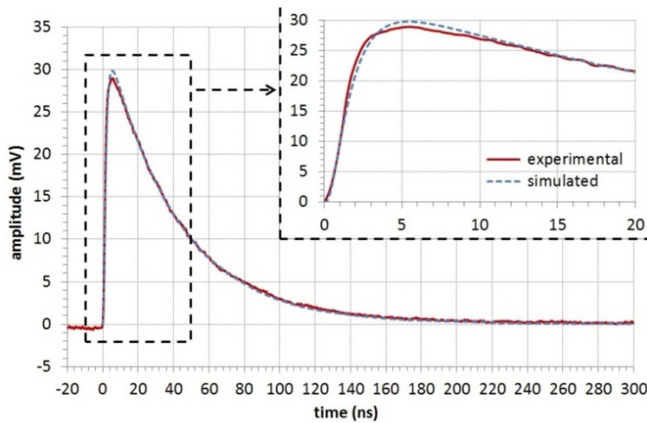


Fig. 6. Simulated and experimental SiPM single-photoelectron responses.

Comparison between the SPICE model simulations and the relevant experimental data is displayed in Fig. 6. As shown, a good fitting is achieved, confirming expectations and validating the proposed extraction procedure.

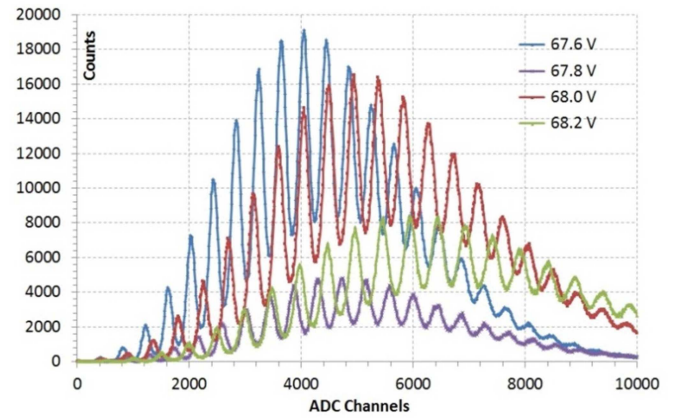


Fig. 7. Charge amplitude histograms at four different bias conditions.

## V. EXPERIMENTAL CROSS-CHECK VALIDATION

In order to further corroborate the effectiveness of the proposed methodology, experimental measurements on the available SiPM device are also carried out following the traditional procedure, to derive some of the SiPM model parameters and compare the achieved results with those extracted in Section IV. In particular, charge measurements are accomplished for a given set of operating voltages, allowing to extract the SiPM gain  $G$ , pixel capacitance  $C_{pixel}$  and breakdown voltage  $V_{BD}$ .

To evaluate the detector gain at a given bias voltage, the integrated charge values generated by a multi-channel analyzer are filled into charge height histograms, and the average spacing between two adjacent curve peaks is computed in terms of ADC channels. As a consequence, accounting for the constant charge/channel rate, and scaling by the pre-amplifier gain factor, the SiPM gain is obtained for a fixed operating condition. During charge measurements, the SiPM device is illuminated with a PDL-200B pulsed diode laser triggering the device microcells. For each acquisition, laser radiation intensity and integration time windows are designed in order to attain a sufficiently large number of photoelectron peaks. Fig. 7 illustrates the SiPM charge measurements at four different bias voltages. The average spacing between succeeding peaks almost linearly increases with the operating conditions.

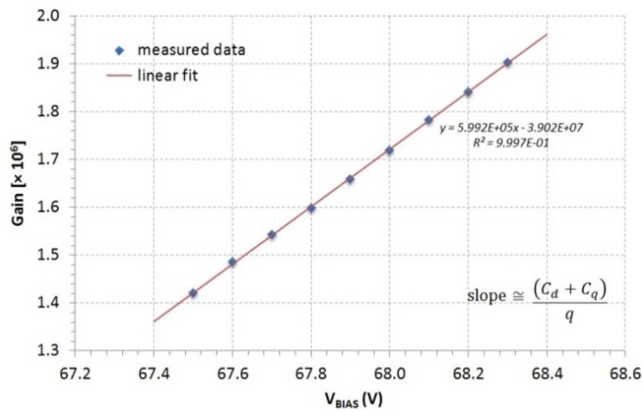


Fig. 8. Gain measurements as a function of the operating voltage. The linear fit allows to extrapolate the breakdown potential.

The SiPM measured gains for a few different bias voltages are plotted in Fig. 8. In particular, a value of  $(1.72 \pm 0.05) \times 10^6$  is estimated at  $V_{BIAS} = 68V$ , which is fairly compatible with the SiPM gain  $G$  extracted in Table I.

Through the slope of the linear fit in a gain graph as a function of the operating voltage, the SiPM pixel capacitance  $C_{pixel}$  can be appraised, in accordance with (4). From Fig. 8, a value of  $(98 \pm 1)fF$  is achieved, which is consistent with the extracted parameters  $C_d$  and  $C_q$  in Table II.

Lastly, the extrapolation of the  $x$ -axis intercept of the linear fit in Fig. 8 provides an estimate of the SiPM breakdown potential, as predicted in (4). As a result, a  $V_{BD}$  of  $(65.1 \pm 0.1)V$  is found, complying with the corresponding datum in Table II.

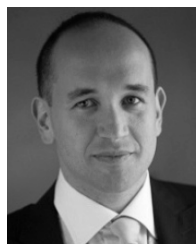
Therefore, the SiPM parameters extracted by the traditional measurement steps are verified to yield good agreement with those assessed following the simpler extraction methodology in Section IV, thus cross-checking the proposed procedure.

## VI. CONCLUSION

In this contribution, an original and simple extraction procedure for deriving the electrical parameters of a SiPM detector has been presented, based on a recently available model of the SiPM device when coupled to its read-out electronics. After a brief review of the analytical analysis developed for determining the complete expression of the single-photoelectron output response, the novel extraction procedure has been proposed, entailing few simple and straightforward measurement steps. The adopted technique has been exploited to extract the electrical parameters of a  $3mm \times 3mm$  Hamamatsu device and construct a SPICE-level model of the SiPM and related read-out circuit. Comparison between simulated and measurement data, along with experimental cross-check results, have confirmed the effectiveness of the new extraction procedure.

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